# **OPERATOR THEORY ON ANALYTIC FUNCTION SPACES 1 (S21)**

MARIBEL LOAIZA-LEYVA (CENTRO DE INVESTIGACION Y DE ESTUDIOS AVANZADOS DEL IPN, MEXICO), RAUL QUIROGA BARRANCO (CIMAT, GUANAJUATO), ARMANDO SANCHEZ-NUNGARAY (UNIVERSIDAD VERACRUZANA), KEHE ZHU (STATE UNIVERSITY OF NEW YORK AT ALBANY)

## (PLT1) chair: Maribel Loaiza-Leyva

Monday 14:	<b>1:00-16:00</b> (P	LT1) chair: Maribel Loaiza-Leyva
14:00-14:25	Nina Zorboska Measure induced Hankel and Toeplitz type opera spaces	tors on weighted Dirichlet
14:30-14:55	hazaleh Asghari Chatten class Hankel operators on doubling Fock spaces and the Berger-Coburn Chenomenon	
15:00-15:25	Cezhong Tong A new class of Carleson embeddings	
15:30-15:55	Zengjian Lou Carleson embedding on Bergman spaces with appli	cations
Monday 16:	<b>5:30-19:00</b> (PL	$\Gamma 1$ ) chair: Raul Quiroga-Barranco
16:30-16:55	Wolfram Bauer Operators in the Fock-Toeplitz Algebra	
17:00-17:25	Robert Fulsche A Wiener algebra on the Fock space	
17:30-17:55	Egor Maximenko Horizontal Fourier transform of the polyanalytic Fock kernel	
18:00-18:25	Stephen Sontz Non-commutative Toeplitz Quantization of Euclidean Planes	
18:30-18:55	Pindoli Mohan Von Neumann algebras of analytic functions on the unit ball	
Tuesday 14:	<b>!:00-16:00</b> (PLT1)	chair: Armando Sanchez-Nungaray
14:00-14:25	Jari Taskinen Bergman projection induced by radial weight acting	g on growth spaces
14:30-14:55	Maribel Loaiza-Leyva On $C^*$ -algebras generated by Toeplitz operators and projections	
15:00-15:25	Shubham Rameshsingh Bais Integral representation of angular operators on the Bergman space over the upper half-plane	
15:30-15:55	Miron Bekker On Generators of the Hardy and the Bergman Spa	ces
Tuesday 16:	<b>3:30-19:00</b> (P	LT1) chair: Maribel Loaiza-Leyva
16:30-16:55	Jani Virtanen	
	Asymptotics of determinants for structured matrices	
17:00-17:25	Zeljko Cučković A geometric condition for the invertibility of Toeplitz operators on the Bergman	
17:30-17:55	space Hyungwoon Koo	
18:00-18:25	Hicham Arroussi Generalized Volterra type integral operators on large	ge Bergman spaces

## $\mathbf{2}$

## Wednesday 11:40-12:40

11:40-12:05

12:10-12:35

To eplitz Operators with symbols invariant under the action of a subgroup of the nilpotent group on the Siegel Domain  $D_2$ 

## Thursday 14:00-16:00

(PLT1) chair: Armando Sanchez-Nungaray

(PLT1) chair: Raul Quiroga-Barranco

# 14:00-14:25 Ching-on Lo Complex Symmetric Weighted Composition-Differentiation Operators on Weighted Hardy Spaces 14:30-14:55 Marek Ptak Invariant Subspaces for conjugations with special behavior with respect to given unitary operator 15:00-15:25 Anusree Sreedharan Multiresolution Analysis on the Weighted Bergman spaces

Abstracts.

#### Hicham Arroussi, University of Reading and Helsinki

Generalized Volterra type integral operators on large Bergman spaces

**Abstract.** : Let  $\phi$  be an analytic self-map of the open unit disk  $\mathbb{D}$  and g analytic in  $\mathbb{D}$ . We characterize boundedness and compactness of generalized Volterra type integral operators

$$GI_{(\phi,g)}f(z) = \int_0^z f'(\phi(\xi)) g(\xi) d\xi$$

and

$$GV_{(\phi,g)}f(z) = \int_0^z f(\phi(\xi)) g(\xi) d\xi$$

acting between large Bergman spaces  $A^p_{\omega}$  and  $A^q_{\omega}$  for  $0 < p, q \leq \infty$ . To prove our characterizations, which involve Berezin type integral transforms, we use the Littlewood-Paley formula of Constantin and Peláez and establish corresponding embedding theorems, which are also of independent interest. When  $\phi(z) = z$ , our results for  $GV_{(\phi,g)}$  complement the descriptions of Pau and Peláez.

#### Ghazaleh Asghari, University of Reading

Schatten class Hankel operators on doubling Fock spaces and the Berger-Coburn phenomenon

**Abstract.** Using the notion of integral distance to analytic functions, we give a characterization of Schatten class Hankel operators acting on doubling Fock spaces on the complex plane and use it to show that for  $f \in L^{\infty}$ , if  $H_f$  is Hilbert-Schmidt, then so is  $H_{\bar{f}}$ . This property is known as the Berger-Coburn phenomenon. When  $0 , we show that the Berger-Coburn phenomenon fails for a large class of doubling Fock spaces. Along the way, we illustrate our results for the canonical weights <math>|z|^m$  when m > 0.

#### References

[1] G. Asghari, Z. Hu, J. A. Virtanen, Schatten class Hankel operators on doubling Fock spaces and the Berger-Coburn phenomenon, J. Math. Anal. Appl. 540, (2024).

#### Shubham R. Bais, The Institute of Mathematical Sciences

Integral representation of angular operators on the Bergman space over the upper half-plane

**Abstract.** Let  $\Pi$  denote the upper half-plane and  $\mathcal{A}^2(\Pi)$  be the Bergman space over the upper half-plane. In this talk, we define a class of integral operators on the space  $\mathcal{A}^2(\Pi)$ . We characterize the integral kernels so that the operators are bounded. We show that this class coincides with the class of angular operators on  $\mathcal{A}^2(\Pi)$ . As a consequence, we discuss various operator theoretic properties of angular operators, and a  $C^*$ -subalgebra generated by Toeplitz operators with special symbols. This is based on the joint work with D. Venku Naidu [1].

#### References

[1] S. R. Bais and D. Venku Naidu, Integral representation of angular operators on the Bergman space over the upper half-plane, *New York J. Math.* **30** (2024), paper no. 4, 42–57 (2024).

## Wolfram Bauer, Leibniz Universität Hannover

## Operators in the Fock-Toeplitz Algebra

**Abstract.** We consider various classes of bounded operators on the Fock space of Gaussian square integrable entire functions over the complex plane. These include Toeplitz (type) operators, weighted composition operators, singular integral operators, Volterra-type operators and Hausdorff operators. As a leading problem and closely linked to well-known compactness or boundedness characterizations we pursue the question of when these operators are contained in the Toeplitz algebra. Some new proofs from the perspective of quantum harmonic analysis will be explained. This is joint work with Robert Fulsche and Miguel A. Rodriguez Rodriguez.

## Miron Bekker, University of Pittsburgh at Johnstown

On Generators of the Hardy and the Bergman Spaces

**Abstract.** A function  $\varphi$  which is analytic and bounded in the unit disk  $\mathbb{D}$  is called a generator for the Hardy space  $H^2(\mathbb{D})$  or the Bergman space  $A^2(\mathbb{D})$  if polynomials in  $\varphi$  are dense in the corresponding space. We characterize generators in terms of  $\varphi$ -invariant subspaces which are also z-invariant and study wandering properties of such subspaces. Density of bounded analytic functions in the  $\varphi$ -invariant subspaces is also investigated.

#### References

[1] John Akeroyd, Density of the polynomials in the Hardy space of certain slit domains. Proceeding of the AMS, **15** (1992), No 4, 1013-1021.

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## Željko Čučković, University of Toledo, USA

A geometric condition for the invertibility of Toeplitz operators on the Bergman space

Abstract. Invertibility of Toeplitz operators on the Bergman space and the related Douglas problem are long standing open problems. In this paper we study the invertibility problem under the novel geometric condition on the image of the symbols, which relaxes the standard positivity condition. We show that under our geometric assumption, the Toeplitz operator  $T_{\varphi}$  is invertible if and only if the Berezin transform of  $|\varphi|$  is invertible in  $L^{\infty}$ . It is well known that the Douglas problem is still open for harmonic functions. We study a class of rather general

harmonic polynomials and characterize the invertibility of the corresponding Toeplitz operators. We also give a number of related results and examples. (Joint work with Jari Taskinen)

## Robert Fulsche, Leibniz Universität Hannover

#### A Wiener algebra on the Fock space

Abstract. In the operator theory of Hardy spaces  $H^p$ , it is well known that the spectrum of the Toeplitz operator  $T_f$  can depend on the precise Hardy space on which the operator is considered, i.e., the spectrum can depend on the choice of the parameter p. In the present talk, we will demonstrate that for Toeplitz operators on the Fock space such behaviour is impossible. More precisely, we will introduce an algebra of integral operators  $\mathcal{W}_t$  (called the *Wiener algebra*), which act boundedly on each of the Fock spaces  $F_t^p$ ,  $1 \leq p \leq \infty$ , and contains all Toeplitz operators with bounded symbols. As the main results, we show that the spectrum, the essential spectrum, and the Fredholm index of an operator from  $\mathcal{W}_t$  do not depend on the choice of the parameter p.

#### Hyungwoon Koo, Korea University

Local Hopf lemma for degenerate elliptic operator

Abstract. We prove that the local Hopf lemma of Baouendi-Rothschild for harmonic functions continues to hold for the degenerate elliptic operator,  $\mathcal{L}_{\alpha} = x^{\alpha} \partial_x^2 + \sum_{j=1}^n \partial_{y_j}^2$ , on the half-space when the degeneracy exponent  $\alpha$  is less than 2. We provide examples of degenerate elliptic operators with the degeneracy exponent greater or equals to 2 for which the local Hopf lemma fail.

#### References

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## Ching-on LO, College of Professional and Continuing Education, The Hong Kong Polytechnic University

## Complex Symmetric Weighted Composition-Differentiation Operators on Weighted Hardy Spaces

Abstract. Complex symmetric weighted composition-differentiation operators on the weighted Hardy spaces  $H^2(\beta)$  with respect to the standard conjugation are investigated. Our results partially answer a question from a paper of Lim and Khoi (2018) [1] and subsume several existing ones in the literature. We also study the classes of self-adjoint, normal, co-isometric, unitary weighted composition-differentiation operators on  $H^2(\beta)$  and their relations with the property of complex symmetry. The talk is based on joint work with Anthony Wai-keung LOH.

#### References

[1] R. Lim and L. H. Khoi, 'Complex symmetric weighted composition operators on  $\mathcal{H}_{\gamma}(\mathbb{D})$ ', J. Math. Anal. Appl. 464, (2018), 101–118.

## Maribel Loaiza-Leyva, Centro de investigación y de estudios avanzados del IPN

On  $C^*$ -algebras generated by Toeplitz operators and projections

Abstract. The C\*-algebra generated by Toeplitz operators, acting on the poly-Bergman space of order n, with bounded vertical symbols (and with finite limits at the points 0 and  $\infty$ ), is isomorphic and isometric to the algebra  $\{M(x) \in M_n(\mathbb{C}) \otimes C[0, +\infty] : M(0), M(\infty) \in \mathbb{C}I\}$ . Then this algebra looks close to the C\*-algebra generated by n orthogonal projections. This implies that, inside the algebra of all bounded operators acting on the Poly-Bergman space of order n, there are n orthogonal projections that generate a C\*-algebra close related to the C\*-algebra generated by all Toeplitz operators with vertical symbols. In this talk we construct a family of projections with these characteristics. One of them is in terms of Toeplitz operators. Besides, we study the C\*-algebra  $\mathcal{A}$  generated by a single Toeplitz operator and the orthogonal projections  $P_1, \ldots, P_n$ , where  $P_k$  is the orthogonal projection from the n-poli-Bergman space onto the true poli-Bergman space of order k. It turns out that, if the vertical symbol of the Toeplitz operator is a characteristic function, the C\*-algebra  $\mathcal{A}$  is isomorphic and isometric to the algebra

 $\mathcal{D}_n := \{ M \in M_n(\mathbb{C}) \otimes C[0,\infty] : M(0), M(\infty) \text{ are diagonal matrices} \}.$ 

In particular, this C\*-algebra contains (isometrically) the C\*-algebra generated by all Toeplitz operators with vertical symbols under the conditions given above.

#### References

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#### Zengjian Lou, Shantou University

Carleson embedding on Bergman spaces with applications

**Abstract.** In this talk, we consider Carleson embedding and its applications. We will introduce the recent development of absolutely summing Carleson embedding on Bergman spaces with applications on composition operators (Based on joint work with B. He (FDU), J. Jreis and P. Lefèvre (Université d'Artois, France))

I would like to thank NNSF of China and Li Ka Shing Foundation for their support.

#### References

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#### Egor Maximenko, Instituto Politécnico Nacional (Mexico)

Horizontal Fourier transform of the polyanalytic Fock kernel

Abstract. This is a joint work with Erick Lee-Guzmán, Gerardo Ramos-Vazquez, and Armando Sánchez-Nungaray.

Let  $\mathcal{F} = \mathcal{F}_m(\mathbb{C}^n)$  be the space of *m*-analytic functions on  $\mathbb{C}^n$  square integrable with the Gaussian weight. Its reproducing kernel was recently computed by Youssfi [1]:

$$K_{\mathcal{F}}(w,z) = e^{\langle w,z \rangle} L_{m-1}^{(n)}(|w-z|^2).$$

We construct a new RKHS  $\mathcal{H}$  multiplying all elements of  $\mathcal{F}$  by the weight

$$2^{\frac{n}{2}}e^{-\frac{1}{2}|w|^2-i\langle\operatorname{Re}(w),\operatorname{Im}(w)\rangle}$$

 $\mathcal H$  is invariant under the usual translations in the horizontal direction. The reproducing kernel of  $\mathcal H$  is

$$K_{\mathcal{H}}(w,z) = 2^{n} e^{-\frac{1}{2}|w-z|^{2} - i\langle \operatorname{Re}(w-z), \operatorname{Im}(w+z) \rangle} L_{m-1}^{(n)}(|w-z|^{2}).$$

Then, we compute the Fourier transform of  $K_{\mathcal{H}}$  in the horizontal direction. It decomposes into a sum of products of Hermite functions:

$$\frac{1}{(2\pi)^{\frac{n}{2}}} \int_{\mathbb{R}^n} K_{\mathcal{H}}(u+iv,iy) e^{-i\langle u,\xi \rangle} du_1 \cdots du_n$$
  
=  $2^n \pi^{\frac{n}{2}} \sum_{k_1+\dots+k_n=m-1} \prod_{r=1}^n \psi_{k_r} \left(\frac{\xi_r+2v_r}{\sqrt{2}}\right) \psi_{k_r} \left(\frac{\xi_r+2y_r}{\sqrt{2}}\right)$ 

The number of summands is  $d = \binom{m+n-1}{n}$ . As the main application, we construct an isometric isomorphism  $R: \mathcal{F} \to L^2(\mathbb{R}^n)^d$  that intertwines Weyl translation operators with multiplication operators by characters of  $\mathbb{R}^n$ . Using [2] we show that the corresponding centralizer (i.e., the von Neumann algebra of "vertical" operators in  $\mathcal{F}$ ) is isometrically isomorphic to  $L^2(\mathbb{R})^{d \times d}$ .

The speaker has been supported by CONAHCYT (Mexico) project "Ciencia de Frontera" FORDECYT-PRONACES/61517/2020 and by IPN-SIP projects.

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#### Pinlodi Mohan, Indian Institute of Technology Hyderabad, India

Von Neumann algebras of analytic functions on the unit ball

**Abstract.** This talk answers the challenge posed by Ma and Zhu in [1]. We provide examples of von Neumann algebras of analytic functions over the unit disc as well as over the unit ball. Also, we introduce a novel multiplication operation on the set of all analytic functions over the unit disc, ensuring that this collection forms a \*-algebra of analytic functions over  $\mathbb{D}$ .

#### References

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## David Norrbo, University of Reading

Asymptotic Toeplitzness of weighted composition operators on Abstract Hardy spaces

**Abstract.** How closely related are weighted composition operators to Toeplitz operators? This talk will provide an answer in terms of asymptotic Toeplitzness of weighted composition operators on abstract Hardy spaces on the disk. This class of spaces include the reflexive Hardy spaces and many Hardy-Lorentz and Orlicz spaces.

## Marek Ptak, University of Agriculture in Kraków, Poland

Invariant Subspaces for conjugations with special behavior with respect to given unitary operator

Abstract. For a given unitary operator U we consider conjugation C (antilinear, isometric, involution) such that U is C-symmetric i.e.  $CUC = U^*$ . The subspaces which are invariant for all such conjugations are characterized. It turns out that it is all subspaces which are hyperinvariant for the given unitary operator U. Next, conjugations commuting with a given unitary operator are investigated. The necessary and sufficient condition when such conjugation exists is given. The description of subspaces which are invariant for all commuting conjugation is much complicated. The examples of specific unitary operators are pointed out.

Joint work with J. Mashreghi, W. Ross.

## Armando Sánchez Nungaray, Universidad Veracruzana

To eplitz Operators with symbols invariant under the action of a subgroup of the nilpotent group on the Siegel Domain  ${\rm D}_2$ 

Abstract. In this talk, we consider two types of subgroups of the Nilpotent group of the Siegel Domain of dimension two  $D_2$ . For each of these two subgroups we construct a Bargman-type transform adapted to the action of that subgroup over  $D_2$ , moreover using these Bargman-type transforme, we characterized the Toeplitz operators with invariant symbols under the action of these subgroups. I would like to thank the Harry Potter Foundation for their generous support.

This is a joint work with Nikolai Vasilevski (RIP).

## Stephen Bruce Sontz, CIMAT, Guanajuato, Mexico

Non-commutative Toeplitz Quantization of Euclidean Planes

**Abstract.** We present a way of constructing Hilbert spaces from an algebraic representation of the Euclidean plane. If a certain Harmony condition is satisfied, this is a reproducing kernel Hilbert space of holomorphic functions. Then, together with a symbol space which is a non-commutative algebra and another Harmony condition, we can define Toeplitz operators and the corresponding quantization, which generalize greatly our previous research on this topic. In collaboration with Micho Durdevich.

#### References

Various eprints on arxiv.

#### Anusree Sreedharan, Cochin University of Science and Technology, India

Multiresolution Analysis on the Weighted Bergman spaces

Abstract. We examine rational Blaschke functions that are capable to formulate a Multiresolution on the weighted Bergman space of the open unit disc  $A^2_{\alpha}(\mathbb{D})$ . We construct a rational orthogonal wavelet system that generates the levels of the multiresolution. The levels of the multiresolution are finite dimensional, which makes it easier to find a basis on each level. We can approximate any  $f \in A^2_{\alpha}(\mathbb{D})$  by the projection operator on the  $n^{\text{th}}$  resolution level. The projection will be an interpolation operator and whose coefficients can be computed through the evaluation of f on a given set of points in the unit disc. We extend the results to weighted Bergman space of upper half plane also.

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[2] Pap, M., Schipp, F. The voice transform on the Blaschke group II. Ann. Univ. Sci. Budapest. Sect. Comput. 29, 157 - 173 (2008)

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## Jari Taskinen, University of Helsinki

Bergman projection induced by radial weight acting on growth spaces

Abstract. A radial weight  $\omega$  on the unit disc  $\mathbb{D}$  of the complex plane is said to belong to the class  $\widehat{\mathcal{D}}$ , if satisfies the upper doubling condition

$$\sup_{0 < r < 1} \frac{\widehat{\omega}(r)}{\widehat{\omega}\left(\frac{1+r}{2}\right)} < \infty,$$

where  $\widehat{\omega}(r) = \int_{r}^{1} \omega(s) ds$  denotes the tail integral. Given a weight  $\omega$ , let  $P_{\omega}$  be the Bergman projection in the space  $L^{2}_{\omega}$ , endowed with the  $\omega$ -weighted area measure. For a weight  $\nu$ , denote  $L^{\infty}_{\widehat{\nu}} = \{f : ||f||_{\infty, \nu} = \operatorname{ess\,sup}_{z \in \mathbb{D}} |f(z)|\widehat{\nu}(z) < \infty\}.$ 

Under the general assumption that either  $\omega$  or  $\nu$  belongs to  $\widehat{\mathcal{D}}$ , we give several characterizations of pairs  $(\omega, \nu)$  such that  $P_{\omega}$  is a bounded operator from  $L_{\nu}^{\infty}$  onto its closed subspace  $H_{\nu}^{\infty}$  consisting of analytic functions. The characterizations involve natural conditions on the moments and/or the tail integrals of  $\omega$  and  $\nu$ . Moreover, we solve the analogous problems for the boundedness of  $P_{\omega}$  from  $L_{\nu}^{\infty}$  onto the corresponding weighted Bloch type spaces and also study similar questions for exponentially decreasing radial weights.

This is a report on a joint work with Álvaro Miguel Moreno and José Ángel Peláez, Universidad de Málaga.

#### Cezhong Tong, Hebei University of Technology

## A new class of Carleson embeddings

**Abstract.** In this talk I will introduce a new class of Carleson embeddings for Bergman-type spaces. This extends the embedding of a single derivative to the embedding of a combination of finite derivatives of different orders. As applications, we can use these new Carleson embeddings to characterize the generalized Volterra-type operators on Bergman-type spaces, and to characterize the boundedness and compactness of sums of weighted composition-differentiation operators of different orders.

## Jani Virtanen, University of Reading

## Asymptotics of determinants for structured matrices

**Abstract.** I discuss the determinant asymptotics for structured matrices with focus on Toeplitz and Toeplitz plus Hankel matrices, and also finite sections of Toeplitz operators, generated by matrix-valued symbols that may be smooth or possess singularities. Most of our results have been proved using operator theory but we also compare the operator-theoretic approach with the use of Riemann-Hilbert problems. Some applications to random matrix theory and mathematical physics are also mentioned.

## References

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 E. Basor, T. Ehrhardt, J. A. Virtanen, A survey of asymptotics of determinants for structured matrices, (preprint to be posted on arXiv).

## Nina Zorboska, University of Manitoba

## Measure induced Hankel and Toeplitz type operators on weighted Dirichlet spaces

**Abstract.** I will talk about the boundedness of measure induced Hankel and Toeplitz type operators on weighted Dirichlet spaces, extending the known results for the case of the classical Hardy and Dirichlet spaces. The approach relies on recent results on weak products of complete Nevanlinna-Pick reproducing kernel Hilbert spaces.